

International Journal of Advanced Research in Science, Engineering and Technology

Vol. 8, Issue 8, August 2021

Spectral and Raman Analysis of Pr³⁺ Doped Zinc Lithium Alumino Tungsten Borophosphate Glasses

S.L.Meena

Ceramic Laboratory, Department of physics, Jai NarainVyas University, Jodhpur 342001(Raj.)India

ABSTRACT: borophosphateglasses Pr^{3+} (40 -Zinc lithium alumino tungsten containing in $x)P_{2}O_{5}:10ZnO:10Li_{2}O:10Al_{2}O_{5}:10WO_{3}:20B_{2}O_{3}:xPr_{6}O_{11}$ (where x=1, 1.5,2 mol %) have been prepared by meltquenching method. The amorphous nature of the glasses was confirmed by x-ray diffraction studies. Optical absorption, fluorescence spectra and Raman spectra were recorded at room temperature for all glass samples. Judd-Ofelt intensity parameters Ω_{λ} (λ =2, 4, 6) are evaluated from the intensities of various absorption bands of optical absorption spectra. Using these intensity parameters various radiative properties like spontaneous emission probability, branching ratio, radiative life time and stimulated emission cross-section of various emission lines have been evaluated.

KEYWORDS: ZLATBP Glasses, Optical Properties, Judd-Ofelt Theory, Raman analysis.

I. INTRODUCTION

Rare earth ions doped in different glass hosts to achieve favourable potential applications in a variety of optical devices such as lasers, fiber amplifiers, optical, liner, high refractive index, high density, large third order nonlinear optical susceptibility and nonlinear properties [1-5]. Phosphate glass is an extremely promising material for laser and nonlinear applications in optics due to some of its essential characteristic features, such as low phonon maxima, low melting temperature and excellent transparency in the far infrared region [6-10].

Phosphate glasses are very important because of the possibility of their application in optoelectronic and optic device fields, such as lasers, fiberopticand solar cells [11-13]. An important characteristic of these materials is the relatively low cutoff phonon energy compared with other oxide glasses such as silicate or tellurite glasses. The addition of network modifier (NWF) Li_2O is to improve both electrical and mechanical properties of such glasses. Zinc oxide is added in the glass matrix to increase glass forming ability and to ensure low rates of crystallization in the glass system [14, 15].

In this work, the spectroscopic properties of Pr^{3+} -doped (40x)P₂O₅:10ZnO:10Li₂O:10Al₂O₃:10WO₃:20B₂O₃:xPr₆O₁₁(where x=1, 1.5,2 mol %) glasses were investigated. The absorption spectra, fluorescence spectra and Raman spectra of Pr^{3+} of the glasses were investigated. The Judd-Ofelt theory has been applied to compute the intensity parameters Ω_{λ} (λ =2, 4, 6).These intensity parameter have been used to evaluate optical optical properties such as spontaneous emission probability, branching ratio, radiative life time and stimulated emission cross section.

II. EXPERIMENTAL TECHNIQUES

A. PREPARATION OF GLASSES

The following Pr^{3+} doped Zinc lithium alumino tungsten borophosphateglasssamples(40-x)P₂O₅:10ZnO:10Li₂O:10Al₂O₃:10WO₃:20B₂O₃:xPr₆O₁₁(where x=1, 1.5.2) have been prepared by melt-quenching method. Analytical reagent grade chemical used in the present study consist of P₂O₅, ZnO, Li₂O,Al₂O₃,WO₃, B₂O₃and Pr₆O₁₁. All weighed chemicals were powdered by using an Agate pestle mortar and mixed thoroughly before each batch (10g) was melted in alumina crucibles in silicon carbide based an electrical furnace.

Silicon Carbide Muffle furnace was heated to working temperature of 1055^oC, for preparation of Zinc lithium alumino tungsten borophosphateglasses, for two hours to ensure the melt to be free from gases. The melt was stirred several times to ensure homogeneity. For quenching, the melt was quickly poured on the steel plate & was immediately



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inserted in the muffle furnace for annealing. The steel plate was preheated $to 100^{\circ}$ C. While pouring; the temperature of crucible was also maintained to prevent crystallization. And annealed at temperature of 350° C for 2h to remove thermal strains and stresses. Every time fine powder of cerium oxide was used for polishing the samples. The glass samples so prepared were of good optical quality and were transparent. The chemical compositions of the glasses with the name of samples are summarized in Table 1

Sample	Glass composition (mol %)	
ZLATBP (UD)	40P ₂ O ₅ :10ZnO:10Li ₂ O:10Al ₂ O ₃ :10WO ₃ :20B ₂ O ₃	
ZLATBP (PR1)	39P ₂ O ₅ :10ZnO:10Li ₂ O:10Al ₂ O ₃ :10WO ₃ :20B ₂ O ₃ :1Pr ₆ O ₁₁	
ZLATBP(PR 1.5)	38.5P ₂ O ₅ :10ZnO:10Li ₂ O:10Al ₂ O ₃ :10WO ₃ :20B ₂ O ₃ : 1.5 Pr ₆ O ₁₁	
ZLATBP (PR2)	38P ₂ O ₅ :10ZnO:10Li ₂ O:10Al ₂ O ₃ :10WO ₃ :20B ₂ O ₃ : 2 Pr ₆ O ₁₁	

ZLATBP (UD)—Represents undopedZinc Lithium Alumino Tungsten Borophosphate glass specimen. ZLATBP(PR) -Represents Pr³⁺ dopedZinc Lithium Alumino Tungsten Borophosphateglass specimens.

III. THEORY

A. OSCILLATOR STRENGTH

The intensity of spectral lines are expressed in terms of oscillator strengths using the relation [16].

$$f_{\text{expt.}} = 4.318 \times 10^{-9} \text{J}\varepsilon (v) \text{ d} v$$

where, ε (*v*) is molar absorption coefficient at a given energy *v* (cm⁻¹), to be evaluated from Beer–Lambert law.

Under Gaussian Approximation, using Beer–Lambert law, the observed oscillator strengths of the absorption bands have been experimentally calculated, using the modified relation [17].

(1)

$$P_{\rm m}=4.6 \times 10^{-9} \times \frac{1}{cl} \log \frac{I_0}{I} \times \Delta \upsilon_{1/2}$$
(2)

where c is the molar concentration of the absorbing ion per unit volume, I is the optical path length, $logI_0/I$ is absorbtivity or optical density and $\Delta v_{1/2}$ is half band width.

B. Judd-Ofelt Intensity Parameters

According to Judd [18] and Ofelt [19] theory, independently derived expression for the oscillator strength of the induced forced electric dipole transitions between an initial J manifold $|4f^N(S, L) J\rangle$ level and the terminal J' manifold $|4f^N(S', L') J\rangle$ is given by:

$$\frac{8\Pi^2 mc\bar{\nu}}{3h(2J+1)n} \left[\frac{(n^2+2)^2}{9} \right] \times S(J,J^{\cdot})$$
(3)
where, the line strength S (J, J') is given by the equation

$$S(J,J) = e^2 \Sigma \Omega_1 < 4f^{N}(S,L)J ||U^{(\lambda)}|| ||4f^{N}(S',L')J'>2$$
(4)

 $S (J, J') = e^{2} \sum \Omega_{\lambda} < 4f^{N}(S, L) J \| U^{(\lambda)} \| 4f^{N}(S', L') J' > 2$ (4) $\lambda = 2, 4, 6$ In the above equation m is the mass of an electron, c is the velocity of light, v is the wave number of the transition,

h is Planck's constant, n is the refractive index, J and J' are the total angular momentum of the initial and final level respectively, Ω_{λ} ($\lambda = 2, 4$ and 6) are known as Judd-Ofelt intensity parameters.

C. Radiative Properties

The Ω_{λ} parameters obtained using the absorption spectral results have been used to predict radiative properties such as spontaneous emission probability (A) and radiative life time (τ_R), and laser parameters like fluorescence branching ratio (β_R) and stimulated emission cross section (σ_p).



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The spontaneous emission probability from initial manifold $|4f^{N}(S', L') J'>$ to a final manifold $|4f^{N}(S,L) J>|$ is given by:

A [(S', L') J'; (S,L)J] =
$$\frac{64 \pi^2 \nu^3}{3h(2J'+1)} \left| \frac{n(n^2+2)^2}{9} \right| \times S(J',\bar{J})$$
 (5)
Where, S (J', J) = $e^2 \left[\Omega_2 \right] ||U^{(2)}||^2 + \Omega_4 ||U^{(4)}||^2 + \Omega_6 ||U^{(6)}||^2]$

The fluorescence branching ratio for the transitions originating from a specific initial manifold $|4f^{N}(S', L') J\rangle$ to a final many fold $|4f^{N}(S,L)J\rangle$ is given by

(6)

(7)

(10)

$$\beta[(S', L') J'; (S, L) J] = \sum \frac{A[(S'L)]}{A[(S'L')J'(\bar{S}L)]}$$

SLJ

where, the sum is over all terminal manifolds.

The radiative life time is given by

$$\tau_{rad} = \sum A[(S', L') J'; (S,L)] = A_{Total}^{-1}$$

S L J
where, the sum is over all possible terminal manifolds. The stimulated

where, the sum is over all possible terminal manifolds. The stimulated emission cross -section for a transition from an initial manifold $|4f^{N}(S', L') J'>$ to a final manifold $|4f^{N}(S,L)J>|$ is expressed as

$$\sigma_p(\lambda_p) = \left[\frac{\lambda_p^4}{8\pi c n^2 \Delta \lambda_{eff}}\right] \times A[(S', L')J'; (\bar{S}, \bar{L})\bar{J}]$$
(8)

where, λ_p the peak fluorescence wavelength of the emission band and $\Delta \lambda_{eff}$ is the effective fluorescence line width.

D.Nephelauxetic Ratio (β) and Bonding Parameter ($b^{1/2}$)

The nature of the R-O bond is known by the Nephelauxetic Ratio (β') and Bonding Parameters ($b^{1/2}$), which are computed by using following formulae [20, 21]. The Nephelauxetic Ratio is given by

$$\beta' = \frac{\nu_g}{\nu_a} \tag{9}$$

where, v_a and v_g refer to the energies of the corresponding transition in the glass and free ion, respectively. The values of bonding parameter $b^{1/2}$ are given by

$$b^{1/2} = \left\lfloor \frac{1-\beta'}{2} \right\rfloor^{1/2}$$

III. RESULT AND DISCUSSION

A. XRD Measurement

Figure 1 presents the XRD pattern of the samples containing show no sharp Bragg's peak, but only a broad diffuse hump around low angle region. This is the clear indication of amorphous nature with in the resolution limit of XRD instrument.



Fig.1:X-ray diffraction pattern of ZLATBP (PR) glasses.



International Journal of Advanced Research in Science, Engineering and Technology

ISSN: 2350-0328

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B. Raman spectra

The Raman spectrum of Zinc Lithium Alumino Tungsten Borophosphate(ZLATBP) glass specimens is recorded and is shown in Fig. 2. The spectrum peaks located at 397 and 777 cm⁻¹. The band at 397 cm⁻¹ is related to the bending motion of phosphate polyhedral PO₄ units with cation like ZnO as the modifier. The broad band at 777 cm⁻¹ is due to symmetric stretching of (P–O–P) bridging oxygen bonds in (P₂O₇)₄ units.



C. Absorption spectra

The absorption spectra of ZLATBP (PR) glasses, consists of absorption bands corresponding to the absorptions from the ground state ${}^{3}H_{4}$ of Pr^{3+} ions. Eight absorption bands have been observed from the ground state ${}^{3}H_{4}$ to excited states ${}^{3}F_{2}, {}^{3}F_{3}, {}^{3}F_{4}, {}^{1}G_{4}, {}^{1}D_{2}, {}^{3}P_{0}, {}^{3}P_{1}$ and ${}^{3}P_{2}$ for Pr^{3+} doped ZLATBP (PR) glasses.



Fig.3: Absorption spectra of ZLATBPPR(01) glass.

The experimental and calculated oscillator strengths for Pr^{3+} ions Zinc lithium alumino tungsten borophosphateglasses are given in **Table 2**



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Energy level	Glass ZLATBP		Glass ZLATBP		Glass ZLATBP	
$^{3}\text{H}_{4}$	(PR01)		(PR1.5)		(PR02)	
	P _{exp.}	P _{cal.}	P _{exp.}	P _{cal.}	P _{exp.}	P _{cal.}
${}^{3}F_{2}$	4.24	3.63	3.75	3.29	2.87	2.46
${}^{3}F_{3}$	7,73	6.78	6.44	5.64	4.86	4.16
${}^{3}F_{4}$	4.25	4.09	3.25	3.35	2.36	2.50
$^{1}G_{4}$	0.48	0.35	0.38	0.29	0.29	0.21
$^{1}D_{2}$	3.35	1.19	2.24	0.99	1.45	0.73
$^{3}P_{0}$	4.48	2.17	3.48	1.89	2.68	1.33
${}^{3}P_{1}$	4.88	3.52	3.77	3.05	2.79	2.17
${}^{3}P_{2}$	11.39	3.97	10.43	3.26	9.39	2.42
R.m.s.deviation	2.9227		2.6667		2.5488	

Table 2.Measured and calculated oscillator strength $(P^m \times 10^{+6})$ of Pr^{3+} ions in ZLATBP glasses.

The various energy interaction parameters like Slater-Condon parameters $F_k(k=2, 4, 6)$, Lande' parameters ξ_{4f} and Racah parameters $E^k(k=1, 2, 3)$ have been computed using partial regression method. The ratio of Racah parameters E^1/E^3 and E^2/E^3 are about 9.79 and 0.048 respectively. Computed values of Slater-Condon, Lande, Racah, nephelauexetic ratio and bonding parameter for Pr^{3+} dopedZLATBP glassspecimens are given in **Table 3**.

Table3.Computed values of Slater-Condon, Lande, Racah, nephelauexetic ratio and bonding parameter for Pr³⁺ doped ZLATBP glass specimens.

Parameter	Free ion	ZLATBPPR01	ZLATBPPR1.5	ZLATBPPR02
$F_2(cm^{-1})$	322.09	300.03	299.99	300.02
$F_4(cm^{-1})$	44.46	44.28	44.25	44.28
$F_6(cm^{-1})$	4.867	4.414	4.410	4.413
$\xi_{4f}(cm^{-1})$	741.00	858.25	858.70	858.28
$E^{1}(cm^{-1})$	4728.92	4451.77	4450.22	4451.45
$E^{2}(cm^{-1})$	24.75	22.01	22.01	22.01
$E^{3}(cm^{-1})$	478.10	454.73	454.72	454.72
F_4/F_2	0.13805	0.14751	0.14751	0.14758
F_6/F_2	0.01511	0.01471	0.01470	0.01471
E^1/E^3	9.8911	9.7899	9.7867	9.7894
E^2/E^3	0.0518	0.0484	0.0484	0.0484
β'		0.88887	0.88849	0.88879
b ^{1/2}		0.23573	0.23613	0.23580

Judd-Ofelt intensity parameters $\Omega_{\lambda}(\lambda = 2, 4 \text{ and } 6)$ were calculated by using the fitting approximation of the experimental oscillator strengths to the calculated oscillator strengths with respect to their electric dipolecontributions. In the present case the three Ω_{λ} parameters follow the trend $\Omega_2 < \Omega_4 < \Omega_6$.

The values of Judd-Ofelt intensity parameters are given in Table 4.



ISSN: 2350-0328 International Journal of Advanced Research in Science, Engineering and Technology

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Glass Specimen	$\Omega_2(pm^2)$	$\Omega_4(\text{pm}^2)$	$\Omega_6(\text{pm}^2)$	Ω_4/Ω_6
ZLATBP (PR01)	2.127	3.265	6.140	0.5318
ZLATBP(PR1.5)	2.064	2.847	5.005	0.5688
ZLATBP(PR02)	1.609	2.003	3.732	0.5367

Table 4.Judd-Ofelt intensity parameters for Pr³⁺ doped ZLATBP glass specimens.

D. Fluorescence Spectrum

The fluorescence spectrum of Pr^{3+} doped in zinc lithium alumino tungsten borophosphateglass is shown in Figure 4. There are eightbroad bands $({}^{3}P_{0} \rightarrow {}^{3}H_{4})$, $({}^{3}P_{1} \rightarrow {}^{3}H_{5})$, $({}^{1}D_{2} \rightarrow {}^{3}H_{4})$, $({}^{3}P_{0} \rightarrow {}^{3}H_{6})$, $({}^{3}P_{0} \rightarrow {}^{3}F_{2})$, $({}^{3}P_{1} \rightarrow {}^{3}F_{3})$, $({}^{1}D_{2} \rightarrow {}^{3}H_{5})$ and $({}^{3}P_{0} \rightarrow {}^{3}F_{4})$ respectively for glass specimens.



Fig.4:Fluorescence spectrum of ZLATBP PR (01) glass.

Table 5.Emission peak wave lengths (λ_p), radiative transition probability (A_{rad}), branching ratio (β_R), stimulated emission crosssection (σ_p), and radiative life time (τ) for various transitions in Pr³⁺ doped ZLATBP glasses.

Transition	ZLATBPPR 01					ZLATBPPR 1.5				ZLATBPPR 02			
	λ_{max}	$A_{rad}(s^{-1})$	β	σ_{p}	$\tau_{\rm R}(\mu s)$	$A_{rad}(s^{-1})$	β	σ_{p}	$\tau_{\rm R}$ (µs)	$A_{rad}(s^{-1})$	β	σ_{p}	$\tau_{\rm R}(10^{-1}$
	(nm)			(10-20				(10^{-20})				(10-20	$^{20} \mathrm{cm}^2$)
				cm ²)				cm ²)				cm ²)	· · ·
$^{3}P_{0}\rightarrow ^{3}H_{4}$	485	1716.00	0.1693	1.062		1500.02	0.1656	1.216		1057.45	0.1579	1.055	
${}^{3}P_{1} \rightarrow {}^{3}H_{5}$	532	2818.32	0.2781	0.6708		2401.69	0.2651	0.618		1730.48	0.2583	0.492	
$^{1}D_{1} \rightarrow ^{3}H_{1}$	500	588.02	0.0580	0.28/3		186.35	0.05360	0.258		360.30	0.05380	0.207	1
$D_2 + \Pi_4$	577	500.02	0.0500	0.2045		400.55	0.05507	0.230		500.57	0.05500	0.207	
$^{3}P_{0}\rightarrow ^{3}H_{6}$	602	495.43	0.0488	0.3472	98.687	404.45	0.04465	0.328	110.39	302.18	0.04511	0.274	149.29
0 0												0.27	
${}^{3}P_{0} \rightarrow {}^{3}F_{2}$	643	1483.96	0.1464	2.053	1	1442.87	0.1593	2.514		1127.03	0.1683	2 4 3 9	
-0 -2												2.437	
${}^{3}P_{1} \rightarrow {}^{3}F_{3}$	676	2706.43	0.2671	1.817		2539.33	0.2803	1.884		1920.72	0.2867	1.529	
$^{1}D_{2} \rightarrow ^{3}H_{5}$	685	7.72	0.00076	0.0117	1	6.618	0.00073	0.0127		4.74	0.00071	0.0106	
2 5												0.0100	
${}^{3}P_{0} \rightarrow {}^{3}F_{4}$	730	317.18	0.0313	0.2857]	277.13	0.0306	0.271		195.46	0.0292	0.208	
								-				2.200	



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V. CONCLUSION

In the present study, the glass samples of composition (40-x):P₂O₅:10ZnO:10Li₂O:10Al₂O₃:10WO₃:20B₂O₃:xPr₆O₁₁(where x=1, 1.5, 2 mol %) have been prepared by melt-quenching method. The value of stimulated emission cross-section (σ_p) is found to be maximum for the transition (${}^{3}P_{0} \rightarrow {}^{3}F_{2}$) forglassZLATBP(PR 01), suggesting that glass ZLATBP(PR01) is better compared to the other two glass systemsZLATBP(PR1.5) and ZLATBP(PR02).

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