



Vol. 12, Issue 10, October 2025

A Study on Integer Design of Solutions of Diophantine Equations

$$\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^{\beta}$$

With $\alpha > 0$, $\beta = 1, 2, 3, 4, 5, 6, 7$ and $x < y < w < z$

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ABSTRACT:

This paper focused on a study to find integer design of exponential solutions Diophantine Equation $\alpha(X^4 + Y^4)^2 = (C^2 + D^2)^2(Z^2 - W^2)P^{\beta}$ with $\alpha > 0, \beta = 1, 2, 3, 4, 5, 6, 7$ and

x < y < w < z with Mathematical induction & generation of Pythagorean triplets. Diophantine equations of higher degrees, like the quartic form

 $\alpha(X^4 + Y^4)^2 = (C^2 + D^2)^2(Z^2 - W^2)P^{\beta}$, play a meaningful role in generating special elliptic curves that are crucial for cryptography and secure communications.

for $\beta = 1$, $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P$, having integer design of solution is parameterized by positive integers k and n, with variables defined as:

$$x = k^{n}, y = k^{n+1}, z = k^{n+3}, w = k^{n+2}, p = k^{6n}, \alpha = (1 + k^{4})^{2}(k^{6} - k^{4}), C = 2k^{2},$$

$$D = k^{4} - 1$$

for
$$\beta = 2$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{3n}$,

$$\alpha = (1+k^4)^2(k^6-k^4), C = 2k^2, D = k^4-1.$$

for
$$\beta = 3$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{2n}$,

$$\alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

for
$$\beta = 4$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$,

$$\alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

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Vol. 12, Issue 10, October 2025

for
$$\beta = 5$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{2n}$,

$$\alpha = k^{n}(1 + k^{4})^{2}(k^{6} - k^{4}), C = 2k^{2}, D = k^{4} - 1.$$

for
$$\beta = 6$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$,

$$\alpha = k^{2n}(1 + k^4)^2(k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

for
$$\beta = 7$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$,

$$\alpha = k^{3n}(1 + k^4)^2(k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

KEYWORDS: Diophantine Equation, exponential, Pythagorean triplet, Integer design.

I. INTRODUCTION

Diophantine equations—polynomial equations with integer solutions—are a central topic in number theory. Among their many variants, **exponential Diophantine equations** involve terms where variables appear as exponents. Finding integer solutions to such equations is notably complex and has implications in mathematics, cryptography, and several scientific fields. Historical Context and Theoretical Background

Classical Diophantine Equations: Traditionally, research started with linear and polynomial forms, such as the well-known cases of Pythagorean triples.

Exponential Generalization: The study of exponential forms expanded from these roots, posing questions that often lack general solution methods and in some cases are proven to be undecidable. In this paper, focused to find the general exponential integer solution of

The general exponential integer solution of $\alpha(X^4 + Y^4)^2 = (C^2 + D^2)^2(Z^2 - W^2)P^{\beta}$

With $\alpha > 0$, is derived from fixed value of $\beta = 1, 2, 3, 4, 5, 6, 7$ and x < y < w < z.

II. RESULTS & DISCUSSIONS:

Proportion 1: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 1$$
 is $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)(Z^2 - W^2)P$

Explanation: Let
$$x = k^n$$
, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{6n}$.

Consider
$$\alpha(X^4 + Y^4) = \alpha k^{4n} (1 + k^4)$$
 implies $\alpha(X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^2$

Again consider
$$(Z^2 - W^2)P = k^{8n}(k^6 - k^4)$$
.

It follows that
$$\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P$$
 implies that





Vol. 12, Issue 10, October 2025

$$\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{8n} (k^6 - k^4)$$
 implies $\alpha (1 + k^4)^2 = (C^2 + D^2)^2 (k^6 - k^4)$.

Solve for α , whenever ($C, D, 1 + k^4$) is a Pythagorean Triplet.

From the References [1],[2],[3],[4],[5],[6], we know that

if r is an even number, then $\left(r, \left(\frac{r}{2}\right)^2 - 1, \left(\frac{r}{2}\right)^2 + 1\right)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that $(C, D, 1 + k^4)$ becomes a Pythagorean Triplet with $C = (2k^2)$,

$$D = (k^4 - 1)$$
, implies $C^2 + D^2 = (1 + k^4)^2$. Hence $\alpha = (1 + k^4)^2 (k^6 - k^4)$.

Hence $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P$ having integer design of solution is parameterized by integers k and n, with variables defined as:

$$x = k^n, y = k^{n+1}, z = k^{n+3}, w = k^{n+2}, p = k^{6n}, \alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2,$$

$$D = k^4 - 1$$
.

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = (k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{8n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P = (\mathbf{1} + \mathbf{k}^4)^4 (k^{2n+6} - k^{2n+4}) k^{6n} = \mathbf{k}^{8n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.

Proportion 2: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 2$$
 is $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2)P^2$

Explanation: Let
$$x = k^n$$
, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{3n}$

Consider $\alpha (X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^2$.

Again consider $(Z^2 - W^2)P^2 = k^{8n}(k^6 - k^4)$.

It follows that $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^2$ implies that

 $\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{8n} (k^6 - k^4)$ implies $\alpha (1 + k^4)^2 = (C^2 + D^2)^2 (k^6 - k^4)$. Solve for α , whenever $(C, D, 1 + k^4)$ is a Pythagorean Triplet.





Vol. 12, Issue 10, October 2025

From the References [4],[5],[6],[7],[8], we know that

if r is an even number, then $\left(r, \left(\frac{r}{2}\right)^2 - 1, \left(\frac{r}{2}\right)^2 + 1\right)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that $(C, D, 1 + k^4)$ becomes a Pythagorean Triplet with $C = (2k^2)$,

$$D = (k^4 - 1)$$
. Hence $\alpha = (1 + k^4)^2 (k^6 - k^4)$.

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = (k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{8n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P^2 = (\mathbf{1} + \mathbf{k}^4)^4 (k^{2n+6} - k^{2n+4}) k^{6n} = \mathbf{k}^{8n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.

Proportion 3: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 3$$
 is $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^3$.

Explanation: Let $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{2n}$

Consider $\alpha (X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^2$.

Again consider $(Z^2 - W^2)P^3 = k^{8n}(k^6 - k^4)$.

It follows that $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^3$ implies that

 $\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{8n} (k^6 - k^4)$ implies $\alpha (1 + k^4)^2 = (C^2 + D^2)^2 (k^6 - k^4)$. Solve for α , whenever $(C, D, 1 + k^4)$ is a Pythagorean Triplet.

From the References [9],[10],[1],[2], we know that

if r is an even number, then $\left(r, \left(\frac{r}{2}\right)^2 - 1, \left(\frac{r}{2}\right)^2 + 1\right)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that ($C, D, 1 + k^4$) becomes a Pythagorean Triplet with $C = (2k^2)$,

$$D = (k^4 - 1)$$
. Hence $\alpha = (1 + k^4)^2 (k^6 - k^4)$.





Vol. 12, Issue 10, October 2025

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = (k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{8n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P^3 = (\mathbf{1} + \mathbf{k}^4)^4 (k^{2n+6} - k^{2n+4}) k^{6n} = \mathbf{k}^{8n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.

Proportion 4: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 4$$
 is $\alpha(X^4 + Y^4)^2 = (C^2 + D^2)^2(Z^2 - W^2)P^4$.

Explanation: Let
$$x = k^n$$
, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$

Consider $\alpha (X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^4$.

Again consider $(Z^2 - W^2)P^4 = k^{8n}(k^6 - k^4)$.

It follows that $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)(Z^2 - W^2)P^4$ implies that

 $\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{8n} (k^6 - k^4)$ implies $\alpha (1 + k^4)^2 = (C^2 + D^2)^2 (k^6 - k^4)$. Solve for α , whenever $(C, D, 1 + k^4)$ is a Pythagorean Triplet.

From the References[3],[4],[5], we know that

if r is an even number, then $\left(r, \left(\frac{r}{2}\right)^2 - 1, \left(\frac{r}{2}\right)^2 + 1\right)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that $(C, D, 1 + k^4)$ becomes a Pythagorean Triplet with $C = 2k^2$, $D = k^4 - 1$. Hence $\alpha = (1 + k^4)^2(k^6 - k^4)$.

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = (k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{8n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P^4 = (\mathbf{1} + \mathbf{k}^4)^4 (k^{2n+6} - k^{2n+4}) k^{6n} = \mathbf{k}^{8n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.





Vol. 12, Issue 10, October 2025

Proportion 5: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 5$$
 is $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^5$.

Explanation: Let
$$x = k^n$$
, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$

Consider
$$\alpha (X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^2$$
.

Again consider
$$(Z^2 - W^2)P^5 = k^{9n}(k^6 - k^4)$$
.

It follows that
$$\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^5$$
 implies that

$$\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{9n} (k^6 - k^4)$$
 implies

$$\alpha(1+k^4)^2=(C^2+D^2)^2k^{9n}(k^6-k^4)$$
. Solve for α , whenever $(C,D,1+k^4)$ is a Pythagorean Triplet.

From the References [1],[2],[3],[4], we know that

if r is an even number, then $\left(r, \left(\frac{r}{2}\right)^2 - 1, \left(\frac{r}{2}\right)^2 + 1\right)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that $(C, D, 1 + k^4)$ becomes a Pythagorean Triplet with $C = 2k^2$, $D = k^4 - 1$. Hence $\alpha = k^n (1 + k^4)^2 (k^6 - k^4)$.

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = k^n(k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{9n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P^5 = (\mathbf{1} + \mathbf{k}^4)^4 k^{9n} (k^6 - k^4) = \mathbf{k}^{9n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.

Proportion 6: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 6$$
 is $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^6$.

Explanation: Let
$$x = k^n$$
, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$

Consider
$$\alpha (X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^4$$

Again consider
$$(Z^2 - W^2)P^6 = k^{10n}(k^6 - k^4)$$
.

It follows that
$$\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^4$$
 implies that

$$\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{10n} (k^6 - k^4)$$
 implies

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Vol. 12, Issue 10, October 2025

 $\alpha(1+k^4)^2=(C^2+D^2)^2k^{2n}(k^6-k^4)$. Solve for α , whenever $(C,D,1+k^4)$ is a Pythagorean Triplet.

From the References [1],[2],[3],[4], we know that

if r is an even number, then $(r, (\frac{r}{2})^2 - 1, (\frac{r}{2})^2 + 1)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that $(C, D, 1 + k^4)$ becomes a Pythagorean Triplet with $C = 2k^2$, $D = k^4 - 1$. Hence $\alpha = k^{2n}(1 + k^4)^2(k^6 - k^4)$.

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = k^{2n}(k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{10n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P^6 = (\mathbf{1} + \mathbf{k}^4)^4 k^{10n} (k^6 - k^4) = \mathbf{k}^{10n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.

Proportion 7: A Study on exponential integer solution of above Diophantine Equation at

$$\beta = 7$$
 is $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^7$.

Explanation: Let
$$x = k^n$$
, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$

Consider $\alpha (X^4 + Y^4)^2 = \alpha k^{8n} (1 + k^4)^2$.

Again consider $(Z^2 - W^2)P^7 = k^{11n}(k^6 - k^4)$.

It follows that $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P^7$ implies that

$$\alpha k^{8n} (1 + k^4)^2 = (C^2 + D^2)^2 k^{11n} (k^6 - k^4)$$
 implies

$$\alpha(1+k^4)^2=(C^2+D^2)^2k^{11n}(k^6-k^4)$$
. Solve for α , whenever $(C,D,1+k^4)$ is a Pythagorean Triplet.

From the References[5],[6],[7],[8], we know that

if r is an even number, then $\left(r, \left(\frac{r}{2}\right)^2 - 1, \left(\frac{r}{2}\right)^2 + 1\right)$ is a Pythagorean triplet.

If r is an odd number, then $(r, \frac{r^2-1}{2}, \frac{r^2+1}{2})$ is a Pythagorean triplet.

It implies that $(C, D, 1 + k^4)$ becomes a Pythagorean Triplet with $C = 2k^2$, $D = k^4 - 1$. Hence $\alpha = k^{3n}(1 + k^4)^2(k^6 - k^4)$.

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Vol. 12, Issue 10, October 2025

Verification: Consider LHS

$$\alpha(X^4 + Y^4)^2 = k^{3n}(k^6 - k^4)(1 + k^4)^2(k^{4n} + k^{4n+4})^2 = k^{11n}(k^6 - k^4)(1 + k^4)^4.$$

Consider RHS

$$= (C^2 + D^2)^2 (Z^2 - W^2) P^7 = (\mathbf{1} + \mathbf{k}^4)^4 k^{11n} (k^6 - k^4) = \mathbf{k}^{11n} (k^6 - k^4) (\mathbf{1} + \mathbf{k}^4)^4.$$

Hence LHS = RHS.

III. CONCLUSION

This equation generalizes classical Diophantine problems, blending sums of fourth powers with multiplicative factorizations. While challenging, targeted parametrization and modular analysis can yield solutions. Future work may classify solutions for specific α , β or link to broader number-theoretic frameworks. The parametric framework provides infinite families of solutions by exploiting algebraic identities and modular arithmetic. Future work could explore non-parametric solutions or generalizations to higher exponents.

 $\alpha(X^4 + Y^4)^2 = (C^2 + D^2)^2(Z^2 - W^2)P^{\beta}$, play a meaningful role in generating special elliptic curves that are crucial for cryptography and secure communications.

for $\beta = 1$, $\alpha (X^4 + Y^4)^2 = (C^2 + D^2)^2 (Z^2 - W^2) P$, having integer design of solution is parameterized by positive integers k and n, with variables defined as:

$$x = k^n, y = k^{n+1}, z = k^{n+3}, w = k^{n+2}, p = k^{6n}, \alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2,$$

$$D = k^4 - 1.$$

for
$$\beta = 2$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{3n}$,

$$\alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

for
$$\beta = 3$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{2n}$

$$\alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

for
$$\beta = 4$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$,

$$\alpha = (1 + k^4)^2 (k^6 - k^4), C = 2k^2, D = k^4 - 1.$$

for
$$\beta = 5$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{n+3}$, $w = k^{n+2}$, $p = k^{2n}$,

$$\alpha = k^{n}(1 + k^{4})^{2}(k^{6} - k^{4}), C = 2k^{2}, D = k^{4} - 1.$$

for
$$\beta = 6$$
 then solution $x = k^n$, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$,

$$\alpha = k^{2n}(1 + k^4)^2(k^6 - k^4), C = 2k^2, D = k^4 - 1.$$





Vol. 12, Issue 10, October 2025

for $\beta = 7$ then solution $x = k^n$, $y = k^{n+1}$, $z = k^{2n+3}$, $w = k^{2n+2}$, $p = k^n$,

 $\alpha = k^{3n}(1 + k^4)^2(k^6 - k^4), C = 2k^2, D = k^4 - 1.$

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